# High Resonance Frequency in a Coupled Cavity DFB-LD with Asymmetric Grating Coupling Coefficients by Photon-Photon Resonance

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Abstract- Enhancement of resonance frequency in a coupled cavity DFB-LD with asymmetric grating coupling coefficients by photon-photon resonance is reported. The resonance frequency is 61.3 GHz and the 3-dB down band width is 82.7 GHz when the injected current is only 2.5 times the threshold current.

## I. INTRODUCTION

To achieve high resonance frequencies for high speed direct modulations of semiconductor lasers, push-pull modulations [1]-[4], external injection of intensity modulated light [5], photon-photon resonance [6]-[9] have been studied. In this paper, to obtain a high resonance frequency and stable single longitudinal mode operation simultaneously, a coupled cavity DFB-LD with asymmetric gating coupling coefficients by photon-photon resonance is numerically studied. When the injected current is 2.5 times the threshold current, the resonance frequency  $f_r$  is 61.3 GHz and the 3-dB down bandwidth  $f_{3dB}$  is 82.7 GHz, which are much higher than  $f_r = 37.2$  GHz and  $f_{3dB} = 53.4$  GHz [8], respectively.

II. OPERATING PRINCIPLE AND STRUCTURE Rate equations are written as

$$\begin{split} \frac{\mathrm{d}}{\mathrm{d}t}S_1 &= \Gamma_1 \Big[ G_1 - \beta_1 S_1 - \theta_{12} S_2 \Big] S_1 - \frac{1}{\tau_{\mathrm{ph1}}} S_1, \\ \frac{\mathrm{d}}{\mathrm{d}t}S_2 &= \Gamma_2 \Big[ G_2 - \beta_2 S_2 - \theta_{21} S_1 \Big] S_2 - \frac{1}{\tau_{\mathrm{ph2}}} S_2, \\ \frac{\mathrm{d}}{\mathrm{d}t}n &= \frac{J}{ed} - \Big[ G_1 - \beta_1 S_1 - \theta_{12} S_2 \Big] S_1 \\ &- \Big[ G_2 - \beta_2 S_2 - \theta_{21} S_1 \Big] S_2 - \frac{1}{\tau_{-}} n, \end{split}$$

where  $S_i$  is photon density,  $\Gamma_i$  is an optical confinement factor,  $G_i$  is an amplification rate,  $\beta_i$  is a selfsaturation coefficient,  $\theta_{ij}$  is a cross-saturation coefficient,  $\tau_{phi}$  is photon lifetime where subscripts *i* and *j* are 1 or 2, *n* is carrier concentration, *J* is injected current density, *e* is the elementary charge, *d* is total thickness of active layers,  $\tau_n$  is carrier lifetime. From small-signal analysis for  $S_1 \gg S_2$  the resonance frequency  $f_r$  is obtained

$$f_{\rm r} \simeq \frac{1}{2\pi} \Biggl[ \frac{\partial \, G_1}{\partial n} \frac{S_{10}}{\tau_{\rm ph1}} + \Gamma_1 S_{10} \Gamma_2 S_{20} (2\beta_1 \beta_2 - \theta_{12} \theta_{21}) \Biggr]^{1/2},$$

where  $S_{10}$  and  $S_{20}$  are steady state values of  $S_1$  and  $S_2$ , respectively. The second term in the bracket contributes to enhancement or diminution of resonance frequency. To obtain high resonance frequency, it is important to achieve

$$2\beta_1\beta_2 - \theta_{12}\theta_{21} > 0.$$

To satisfy this condition, a coupled cavity DFB-LD shown in Fig.1 is proposed. Region 1 has phaseshifted gratings with the grating coupling coefficient  $\kappa_1$ =40 cm<sup>-1</sup>, the region length  $L_1$ =300 µm, the corrugation pitch  $\Lambda_1$ =238.45 nm, and the phaseshift  $\Delta\Omega_1 = -\pi$  at the center of Region 1. Region 2 has phase-shifted gratings with the grating coupling coefficient  $\kappa_2$ =33 cm<sup>-1</sup>, the region length  $L_2$ =300 µm, the corrugation pitch  $\Lambda_2$ = $\Lambda_1$ – $\Delta\Lambda$ , and the phase-shift  $\Delta\Omega_2$ = –  $\pi$  at the center of Region 2. Both facets are anti-reflection coated; the power reflectivities  $R_1$  and  $R_2$  are assumed to be zero.



Fig. 1 Analytical model of a coupled cavity DFB-LD with asymmetric grating coupling coefficients. Both facets are anti-reflection coated.

Undoped active layers consist of five 7.5 nmthick  $In_{0.557}Ga_{0.443}As_{-82}P_{0.018}$  strained quantum wells (QWs). These QWs are sandwiched by 23 nm-thick  $In_{0.738}Ga_{0.262}As_{0.568}P_{0.432}$  barriers. The substrate is nInP with impurity concentration of  $10^{18}$ cm<sup>-3</sup>. The upper cladding layer is p-InP with impurity concentration of  $5 \times 10^{17}$ cm<sup>-3</sup>. The waveguide is 1.5  $\mu$ m wide. Region 1 and Region 2 have a common anode and a common cathode.

# **III. SIMULATED RESULTS**

Figure 2 shows the resonance frequency  $f_r$  as a function of the grating pitch difference  $\Delta\Lambda$  for the injected current I = 20 mA. The resonance frequency  $f_r$  has a peak of 53.0 GHz at  $\Delta\Lambda$ =1.6 nm. This  $f_r$  is 6.9 times as high as  $f_r$ =7.68 GHz at  $\Delta\Lambda$ =0 nm.



Fig. 2 Resonance frequency  $f_r$  as a function of the grating pitch difference  $\Delta \Lambda$ .

Figure 3 shows the resonance frequency  $f_r$  as a function of  $I/I_{th}-1$  at  $\Delta\Lambda=1.6$  nm where I is the injected current and  $I_{th}$  is the threshold current. The resonance frequency  $f_r$  increases with  $I/I_{th}-1$ , and the resonance frequency  $f_r$  is 61.3 GHz when  $I/I_{th}-1=1.5$ . When  $I/I_{th}-1$  is larger than 1.5, the stable condition is not satisfied.



Fig.3 Resonance frequency  $f_r$  as a function of the relative bias current  $I/I_{th}-1$ .

Figure 4 shows frequency response for  $\Delta \Lambda$ =1.6 nm and  $I/I_{th}$ -1=1.5. The resonance peak is clearly observed at the modulation frequency of 61.3GHz. The 3-dB down band width is 82.7 GHz.

Figure 5 shows oscillation spectrum for  $\Delta \Lambda = 1.6$  nm and  $I/I_{th} = 1.5$ . The main-mode oscillates at 1.5244 µm which is Bragg wavelength in Region 1. Slight sub-mode exists at 1.5223µm.

Table 1 summarizes  $f_r$  and  $f_{3dB}$  with conditions in the references and the present work.



Table 1  $f_r$  and  $f_{3dB}$  when  $I/I_{th}-1=1.5$ .

$\kappa_2 (\text{cm}^{-1})$	$L_2(\mu m)$	$\Delta\Omega_2$	fr (GHz)	f <sub>3dB</sub> (GHz)	Ref.
40	300	$-\pi$	21.4	31.6	[7]
40	310	0	37.2	53.4	[8]
40	300	-0.9 π	24.3	35.7	[9]
33	300	$-\pi$	61.3	82.7	Pres.

## **IV. CONCLUSIONS**

The coupled cavity DFB-LD with asymmetric grating coupling coefficients was proposed and simulated. For  $\Delta\Lambda$ =1.6 nm and  $I/I_{th}$ -1=1.5, the resonance frequency and the 3-dB down bandwidth were enhanced from 37.2 GHz to 61.3 GHz and from 53.4 GHz to 82.7 GHz, respectively.

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